Further evidence that the sound-speed algorithm of Del Grosso is more accurate than that of Chen and Millero

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Estimates of the bottom depth of the ocean at 11 sites were determined by combining round-trip acoustic travel time measurements made by inverted echo sounders on the ocean bottom with sound-speed profiles determined from simultaneously measured temperature and salinity profiles. These depths were converted into pressures and were compared to independently measured bottom pressures to determine the accuracy of the algorithms used to calculate the sound-speed profile. The sound-speed algorithms tested were those derived by Del Grosso [{\textit{J. Acoust. Soc. Am.} \textbf{56}, 1084–1091 (1974)}] and by Chen and Millero [{\textit{J. Acoust. Soc. Am.} \textbf{62}, 1129–1135 (1977)}], as well as the corrected version of Chen and Millero’s algorithm recently published by Millero and Li [{\textit{J. Acoust. Soc. Am.} \textbf{95}, 2757–2759 (1994)}]. The results of this study agree with the results from recent acoustic tomography experiments which indicate that the algorithm of Del Grosso for the speed of sound in seawater is more accurate than the currently accepted standard algorithm of Chen and Millero. Del Grosso’s algorithm also produces more accurate results than those from the Millero and Li correction to the Chen and Millero algorithm. © 1997 Acoustical Society of America. [S0001-4966(97)05610-5]

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INTRODUCTION

The algorithm of Chen and Millero\textsuperscript{1} for sound speed in seawater is the internationally accepted standard for use with hydrographic data,\textsuperscript{2} however, recent acoustic tomography work by Spiesberger and Metzger,\textsuperscript{3} Dushaw \textit{et al.},\textsuperscript{4} and Spiesberger,\textsuperscript{5} has indicated that the sound-speed algorithm presented in Del Grosso\textsuperscript{6} is more accurate. The two algorithms calculate about the same sound-speed profile in the upper 1000 dbars, but Del Grosso’s algorithm calculates speeds that are slower by about 0.8 m s\textsuperscript{−1} at depths of 5000 dbars. (The unit for pressure used here is the decibar, or dbar for short, which is equal to 10\textsuperscript{4} Pascals. Oceanographers commonly report pressure in dbars rather than the SI units of Pascals because 1 dbar=1 m of depth in the ocean.) Recently, a correction to the Chen and Millero algorithm for low temperatures and high pressures was published by Millero and Li.\textsuperscript{7} This correction reduces the difference between the two algorithms, but the corrected algorithm also consistently predicts higher sound speeds in the deep water than Del Grosso’s algorithm. This study provides further evidence to support Del Grosso’s algorithm by comparing pressures measured by pressure sensors to pressures estimated from acoustic travel time measurements made by inverted echo sounders.

I. DATA

Inverted echo sounders (IESs) are instruments moored about one meter off the ocean bottom that measure the time for 10-kHz pulses to travel the round-trip distance to the ocean surface and back.\textsuperscript{8,9} PIES are IESs that are also equipped with pressure sensors from Paroscientific Inc., which are based on oscillating quartz crystals to which tension is applied via a Bourdon tube.\textsuperscript{10}

II. METHODS

The travel time measurement, \(\tau\), was used to estimate the bottom pressure in the following manner. The round-trip travel time is given by

\[
\tau = 2 \int_{-H}^{0} \frac{1}{c} \, dz,
\]

where \(H\) is the depth of the acoustic transducer and \(c\) is the sound speed. Defining

\[
\left\langle \frac{1}{c} \right\rangle = \frac{1}{H} \int_{-H}^{0} \frac{1}{c} \, dz,
\]

Eq. (1) can be rearranged to give

\[
H = \frac{\tau}{2 \left( \frac{1}{\left\langle c \right\rangle} \right)}.
\]
Sound-speed profiles were calculated from the CTD data using both the Del Grosso (hereafter DG74) and Chen and Millero (hereafter CM77) algorithms as well as the corrected Chen and Millero algorithm (hereafter ML94). These sound-speed profiles were then substituted into Eqs. (2) and (3) along with the concurrent travel times measured by the PIES to calculate the depths (in meters) of the PIES using each of the three sound-speed algorithms. These depths were then converted into pressures by making use of the equation described in Fofonoff and Millard. They give the following equation for converting from pressure to depth,

\[ z = \frac{C_1 p + C_2 p^2 + C_3 p^3 + C_4 p^4}{g(\phi) + \frac{1}{2} \gamma' p} + \frac{\Delta D}{9.8}, \]

where \( C_1 = 9.726 \times 10^2 \), \( C_2 = -2.2512 \times 10^{-5} \), \( C_3 = 2.279 \times 10^{-10} \), \( C_4 = -1.82E-15 \), \( \gamma' = 2.184E-06 \) m s^{-2} dbar^{-1}, \( p \) is the pressure, and \( \Delta D \) is the dynamic height anomaly measured from pressure \( p \) to the surface. This equation was inverted using an iterative method which resulted in pressures that are inherent to the measurements of the pressure sensor located on the PIES. (There are a number of constant offsets that are inherent to the measurements of these instruments which must be accounted for as part of this procedure, as presented in the Appendix.)

### III. ERRORS IN THE MEASURED AND CALCULATED PRESSURES

Before presenting the results of this comparison, a discussion of the errors involved in both the measurement of pressure and the calculation of pressure is in order. All errors quoted throughout this paper are at the one standard deviation level except where otherwise noted. Paroscientific states that the absolute accuracy of the pressure sensor measurement is 0.01% of full scale, about 0.5 dbar for instruments designed for up to 4500-m depths. These Paroscientific pressure sensors have historically had problems with long-term drifts while deployed. However, recent work in the Gulf Stream has indicated that these drifts can be removed quite accurately. The linear drifts in the pressure sensors used here were all below 0.3 dbar per year and most of them were less than 0.05 dbar per year. The travel time measurement of the IES is accurate to 1 ms, which is equivalent to an error in the calculated pressure of 0.75 dbar.

The largest source of error in the calculation results from the spatial offset between the PIES site and the location where the CTD is taken, which introduces random scatter due to the variation of the sound-speed profile caused by lateral gradients and internal waves and tides during the several hours involved in the CTD measurement. These errors are difficult to quantify; however, based on the maximum oceanic thermocline slope and the amplitude of tidal and higher frequency variability observed the combined error estimate is between 0.25 (at a CTD–PIES distance of 0 km) and 2.5 dbar (at a CTD–PIES distance of 3 km). The specific CTD–PIES distances and errors are accounted for in the results section. Finally, errors in the sound-speed equations will also contribute to errors in the calculated pressure.

<table>
<thead>
<tr>
<th>Measured pressure</th>
<th>DG74 (dbars)</th>
<th>CM77 (dbars)</th>
<th>ML94 (dbars)</th>
<th>Number of CTD casts at site</th>
<th>Location</th>
</tr>
</thead>
<tbody>
<tr>
<td>3313.3</td>
<td>3314.3</td>
<td>3315.2</td>
<td>3314.6</td>
<td>3</td>
<td>North Atlantic</td>
</tr>
<tr>
<td>3944.8</td>
<td>3945.3</td>
<td>3946.4</td>
<td>3945.6</td>
<td>2</td>
<td>Current</td>
</tr>
<tr>
<td>4814.0</td>
<td>4816.1</td>
<td>4817.6</td>
<td>4816.5</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>4978.2</td>
<td>4977.9</td>
<td>4979.4</td>
<td>4978.3</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>4812.4</td>
<td>4814.4</td>
<td>4815.9</td>
<td>4814.8</td>
<td>9</td>
<td>Hawaii</td>
</tr>
<tr>
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<td>496.7</td>
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<tr>
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<tr>
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<td>1</td>
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</tr>
<tr>
<td>540.0</td>
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<td>531.4</td>
<td>531.4</td>
<td>N/A</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

DG74 and ML94 both quote an accuracy of 0.05 m s^{-1}, which translates to a maximum potential error in the calculated pressure of about 0.2 dbar. CM77 quotes an accuracy of 0.2 m s^{-1}, resulting in a maximum potential error of about 0.8 dbar in the calculated pressure.

### IV. RESULTS

Table I lists the measured pressures at the 11 PIES sites, together with the mean of the calculated pressures from all CTDs at each site, using CM77, ML94, and DG74. (ML94 was not used to calculate pressures at the shallow sites from the Kuroshio because the correction is for low temperatures and high pressures.) At the shallow (400–1000 m) sites from the Kuroshio, the agreement between the calculated pressures and the measured pressures is generally quite good, and there is little difference between the pressures calculated using DG74 and CM77. This is to be expected since DG74 and CM77 give very similar sound-speed profiles above 1000 dbar. Figure 1A shows that instruments located at shallow depths have calculated pressures about equal to the measured pressures, within the range of the scatter. Because of the good agreement between the calculated and measured pressures at these sites, the rest of this discussion will focus on the differences found at the deep sites.

#### A. Relative differences between algorithms

At depths greater than 3000 m the calculated pressures are consistently higher than the measured pressures. Figures 1B–D show that for these sites the pressures calculated using DG74 are about 1–1.5 dbar closer to the measured pressures than those calculated by CM77. The pressures calculated using ML94 are 0.3–0.4 dbar larger than those from DG74. These differences are significant because the only dissimilarities between the different methods of calculation are the sound-speed algorithms used. The above-quoted sound-speed algorithm accuracies explain a difference of 0.82 dbar between DG74 and CM77 and

\[ \sqrt{0.8^2 + 0.2^2} = 0.82 \text{ dbar between DG74 and CM77 and} \]
\[
\sqrt{0.2^2 + 0.2^2} = 0.28 \text{ dbar between DG74 and ML94. Thus for an individual PIES and CTD pair, the differences between pressures calculated using DG74 and CM77 or DG74 and ML94 would not be significant at the two standard deviation level. It is important to realize, however, that these offsets are appearing in the mean of 17 different CTD and PIES combinations, and thus it is necessary to consider the standard deviation of the mean. Conservatively, it can be said that there are at least five degrees of freedom, one for each independent PIES site, so the standard deviation of the mean can be estimated.}
\]

FIG. 1. Pressure difference \((P_{\text{meas}} - P_{\text{calc}})\) plotted vs \(P_{\text{meas}}\), where pressures calculated using DG74 are denoted by crosses, pressures calculated using CM77 are denoted by circles, and pressures calculated using ML94 are denoted by open boxes. Panel A shows the sites from the Kuroshio, panel B shows the sites near Hawaii, panel C shows the sites in the North Atlantic Current, and panel D shows all of the sites together. Results from all CTDs are shown. Dashed line denotes zero error.
mean offset between DG74 and CM77 is 0.37, and it is 0.13 dbar between DG74 and ML94. Thus even at the two standard deviation level there are statistically significant differences between the pressures calculated using DG74 and those calculated using CM77 and ML94.

### B. Absolute differences between measured and calculated pressures

The mean differences between the measured pressures at the deep sites and those calculated at the same sites using DG74, CM77, and ML94 are 1.4, 2.7, and 1.7 dbar, respectively. The total error (one standard deviation level) estimated for the calculations, due mainly to the spatial offset between the CTD sites and the PIES sites, which have a mean separation of 1.5 km, is 1.5 dbar for the pressure calculations using DG74 and ML94, it is 1.6 dbar for the pressure calculation using CM77. The corresponding standard deviation of the means, once again assuming five degrees of freedom, is about 0.7 dbar for all three algorithms. Thus the differences between the measured pressures and those calculated using DG74 are (barely) not statistically significant at two-standard deviations of the mean, whereas the differences from the pressures calculated using CM77 are nearly twice the size of the 95% errors, and those calculated using ML94 are more than 20% larger than can be accounted for by two standard deviations of the mean. These results indicate that DG74 calculates more accurate sound speeds in the deep ocean than both CM77 and its recently updated version, ML94.

Note, however, that even the pressures calculated by DG74 at the deep North Atlantic Current and Hawaii sites are consistently greater than the measured pressures. The amount by which the vertically averaged sound speed [from Eq. (2)] would need to change to eliminate the difference between measured and calculated pressure can be estimated by rearranging Eq. (3) to give $c/c = \Delta H/H = \Delta p/p$. Figure 2 demonstrates that for nearly all of the sites at depths greater than 3000 dbar, the vertical mean sound-speed needs to be reduced to bring the calculated pressures in line with the measured pressures. This observation is consistent with the results of Spiesberger and Metzger, who found that DG74 calculated speeds that were $0.22 \text{ m s}^{-1}$ too fast at a depth of 3 km. Including the correction from Spiesberger and Metzger in DG74 decreases the calculated pressures by about 0.2–0.4 dbar for the deeper PIES sites (the effect on the shallow Kuroshio sites is negligible). In a later paper Spiesberger questioned his proposed correction by explaining that the offsets he noted could have been due to his model parameters rather than a problem with the DG74 algorithm. Essentially he enlarged his error bars to indicate that he had insufficient information to determine definitively whether DG74 was predicting speeds that were too fast in the deep water. The results of this study indicate that a correction of the same sign and of somewhat larger magnitude than that recommended by Spiesberger and Metzger would give better agreement between the calculated and measured pressures. A decrease in the vertically averaged sound speed of about $0.5 \text{ m s}^{-1}$ would reduce the mean of the observed offsets between the directly measured pressures and the calculated pressures to zero. It is important to note, however, that the pressures calculated using DG74 are not statistically different than the measured pressures based on our estimate of the errors involved in this calculation, so these results cannot definitively state that DG74 is calculating speeds that are too fast. However, since two completely different types of experiments, Spiesberger’s modeling of acoustic tomography data and this study’s comparison of measured pressures to acoustically determined pressures, have both found that DG74 consistently results in deep sound speeds that are too fast, it seems likely that sound speeds calculated at depths greater than 1000 dbar are still too high.

### V. Conclusions

This study involved data from three separate experiments: one in the Kuroshio during 1991–92, the second off Hawaii in 1991–92, and the third in the North Atlantic Current from 1993–95. By directly measuring bottom pressure and comparing it with calculated bottom depth and pressure from travel times measured by inverted echo sounders and sound speed calculated from coinciding full-water-column CTDs, this study has provided additional evidence that Del Grosso’s sound-speed algorithm is more accurate than that of Chen and Millero. Del Grosso’s algorithm provides more accurate velocities at depths even when the recently published correction for low temperatures and high pressures for Chen and Millero’s algorithm is used. The results also suggest that even Del Grosso’s sound-speed algorithm may be calculating speeds that are slightly too fast in water deeper than 1000 dbar. Further measurements would be required to confirm this hypothesis. Nevertheless, Del Grosso’s algorithm is accurate enough to calculate bottom depths and pressures to within about 1 m and 1 dbar in 5000 dbar.

![Figure 2](image-url)
ACKNOWLEDGMENTS

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APPENDIX: INHERENT OFFSETS IN THE PIES

Both the travel time and pressure measurements made by the PIES are subject to some constant offsets which are compensated for here. There is a fixed 3-ms internal response delay in the IES, which must be subtracted from the measured travel time to avoid overestimating the depth of the IES. The pressure sensors measure absolute pressure, rather than gauge pressure, so the atmospheric pressure must be removed from the measured pressure, because the PIES measures the acoustic travel time relative to the sea surface. Since variations of atmospheric pressure are on the order of a tenth of a decabar, it is sufficient to subtract the annual mean regional value of atmospheric pressure (10.2, 10.2, and 10.1 dbar for, respectively, the North Atlantic Current, Hawaii, and Kuroshio regions). Last, the pressure sensor on the PIES is located 0.58 m below the acoustic transducer, so for comparison to the pressure estimated from the travel time, the corresponding small hydrostatic offset (0.60 dbar) was subtracted from the measured pressure.